

Algebra I: Exercises

These notes reflect material from our text, *A First Course in Abstract Algebra, Seventh Edition*, by John B. Fraleigh, published by Addison-Wesley, 2003.

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