

doctors

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January 7, 2016

doctors

references:

- Cannon, et al., Stat2, chapter 01, example 1.6

Import the data.

```
data <- read.csv("MetroHealth83.csv", header=TRUE)
head(data[, c(1, 2, 4)])
```

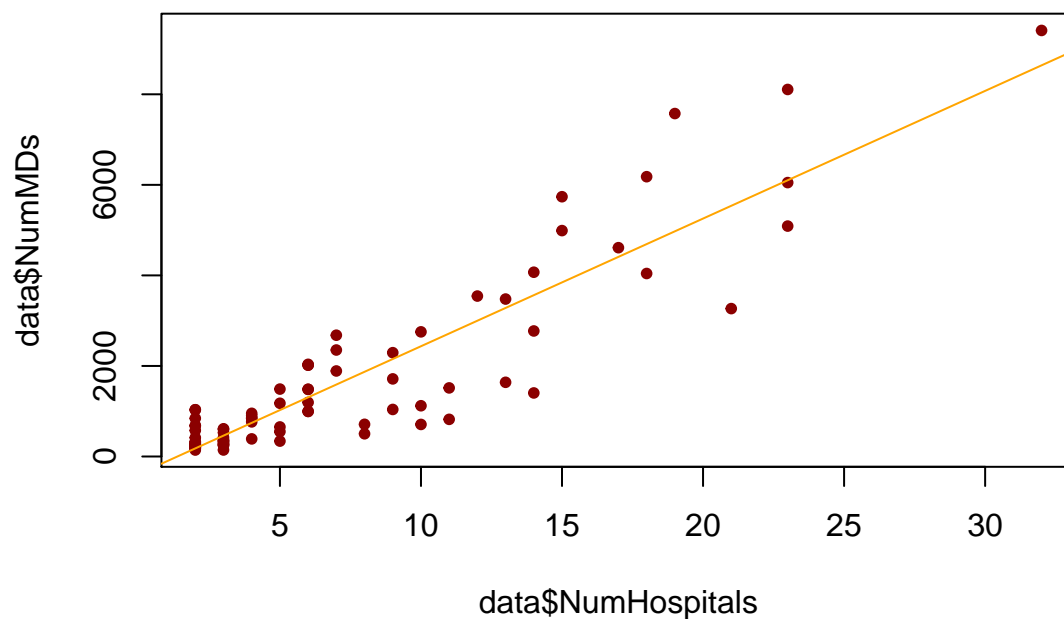
```
##              City NumMDs NumHospitals
## 1  Holland-Grand Haven, MI    349         3
## 2    Louisville, KY-IN   4042        18
## 3    Battle Creek, MI    256         3
## 4          Madison, WI   2679         7
## 5    Fort Smith, AR-OK    502         8
## 6 Sarasota-Bradenton-Venice, FL 2352         7
```

```
dim(data)
```

```
## [1] 83 16
```

View the data.

```
plot(data$NumHospitals, data$NumMDs,
      pch=20, col="darkred")
doctors.lm <- lm(NumMDs ~ NumHospitals, data=data)
abline(doctors.lm, col="orange")
```



Linear model.

$$\widehat{NumMDs} = -385.102 + 282.009 NumHospitals$$

```
options(show.signif.stars=FALSE)
summary(doctors.lm)
```

```
##
## Call:
## lm(formula = NumMDs ~ NumHospitals, data = data)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -2270.09 -263.44   58.08   309.02 2601.93
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)  -385.10     138.26  -2.785  0.00666
## NumHospitals   282.01       14.42  19.563 < 2e-16
##
## Residual standard error: 833.2 on 81 degrees of freedom
## Multiple R-squared:  0.8253, Adjusted R-squared:  0.8232
## F-statistic: 382.7 on 1 and 81 DF,  p-value: < 2.2e-16
```

```
anova(doctors.lm)
```

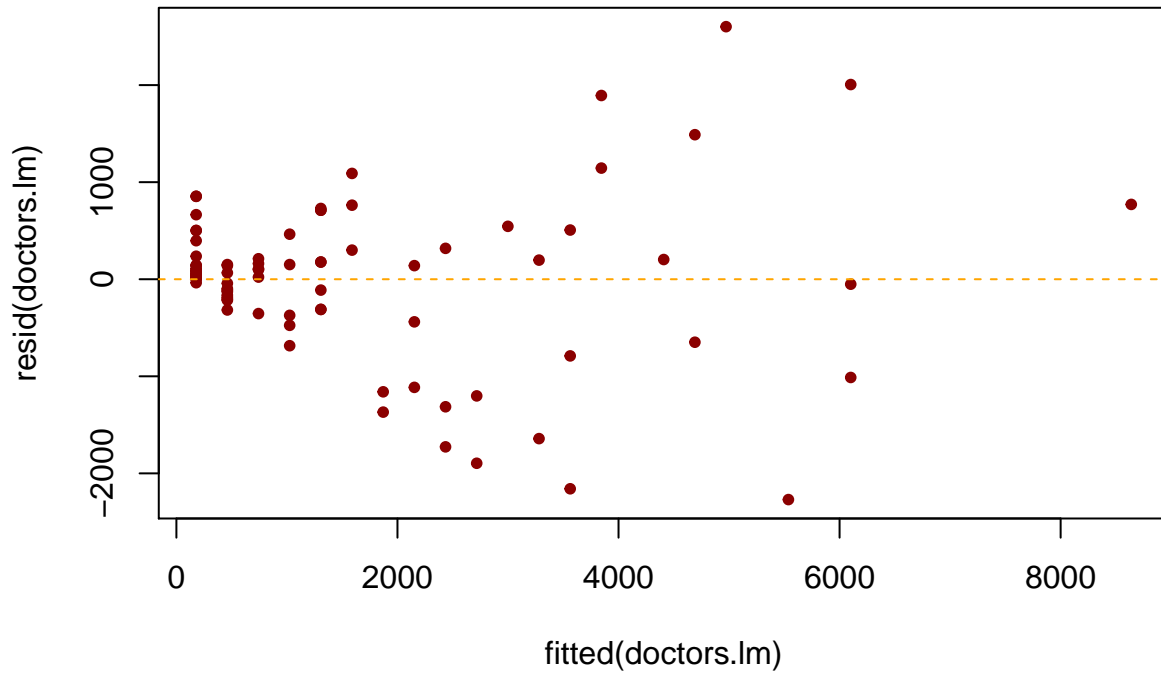
```
## Analysis of Variance Table
##
## Response: NumMDs
##           Df    Sum Sq Mean Sq F value    Pr(>F)
## NumHospitals  1 265700224 265700224  382.69 < 2.2e-16
## Residuals    81  56237663   694292
```

Regression (= residual) standard error.

$$\widehat{\sigma}_e = \sqrt{MSE} = 833.242$$

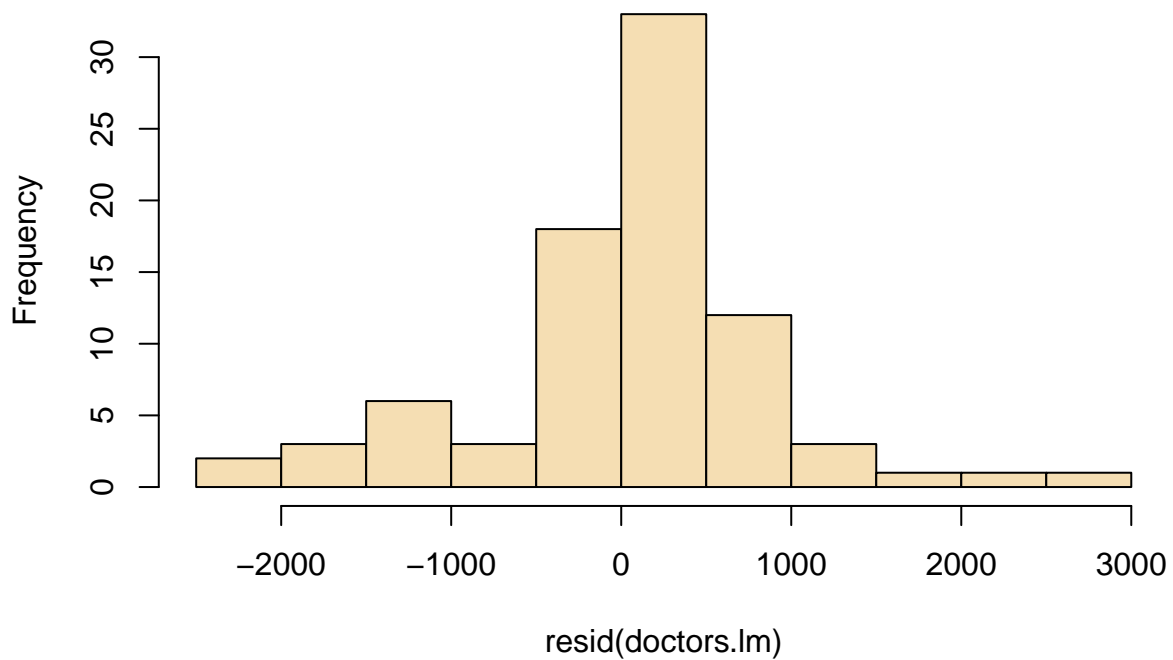
Residuals.

```
plot(fitted(doctors.lm), resid(doctors.lm),
     pch=20, col="darkred")
abline(h=0, col="orange", lty="dashed")
```



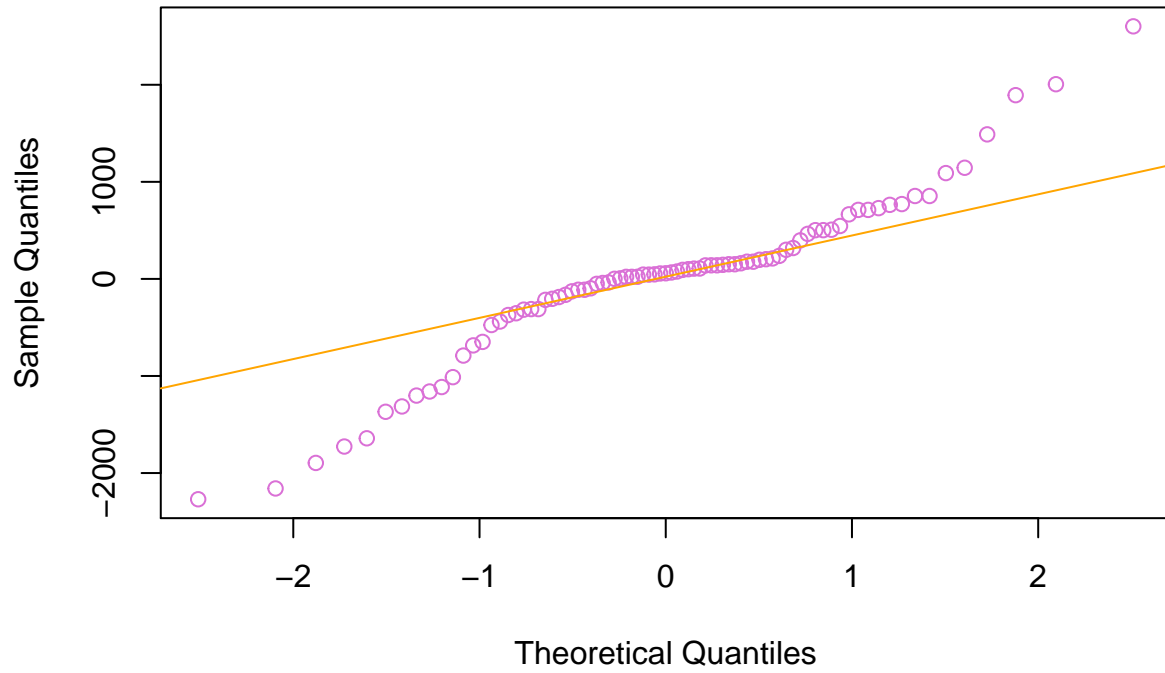
```
hist(resid(doctors.lm), col="wheat")
```

Histogram of resid(doctors.lm)



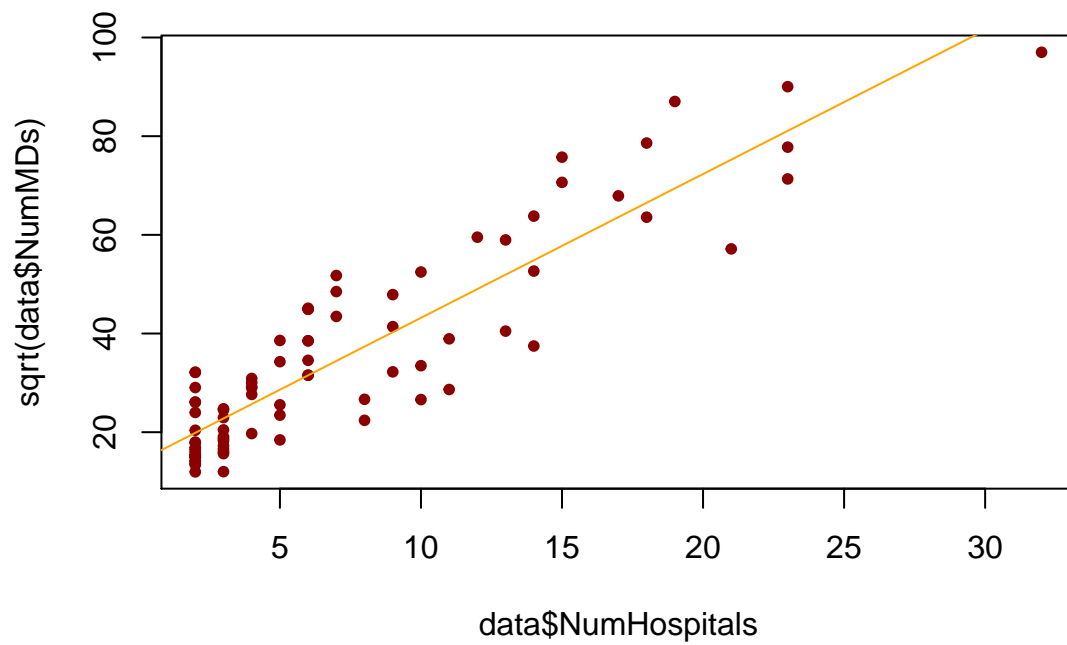
```
qqnorm(resid(doctors.lm),
       col="orchid")
qqline(resid(doctors.lm), col="orange")
```

Normal Q-Q Plot



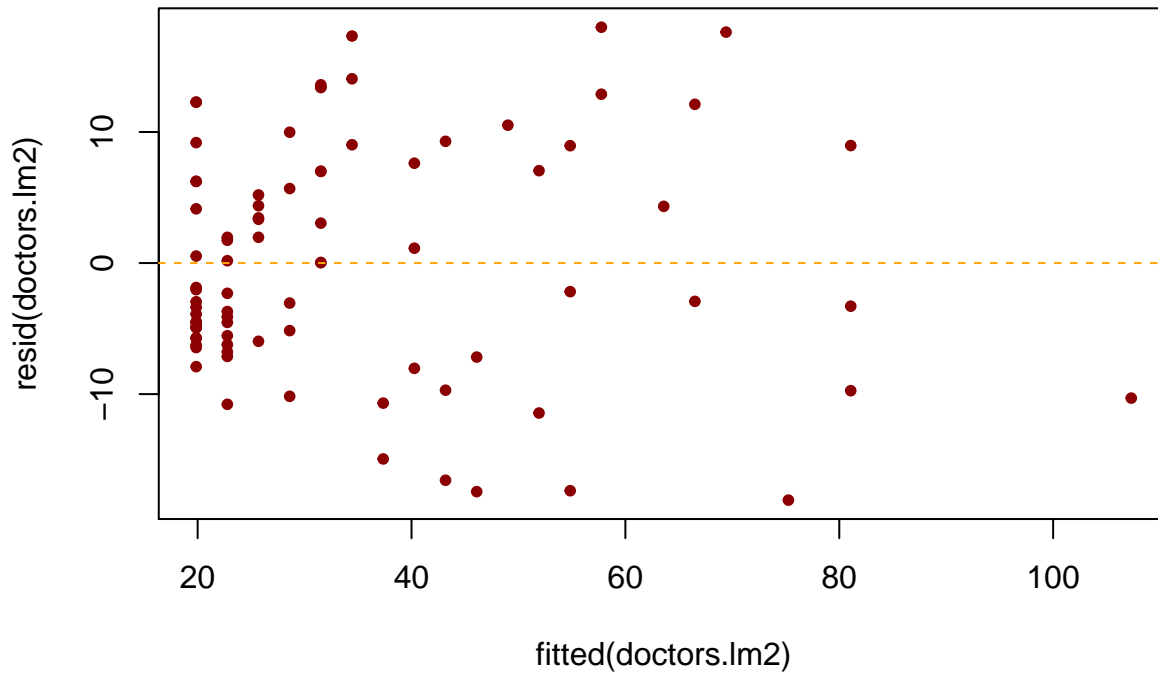
Transformation.

```
plot(data$NumHospitals, sqrt(data$NumMDs),  
     pch=20, col="darkred")  
doctors.lm2 <- lm(sqrt(NumMDs) ~ NumHospitals, data=data)  
abline(doctors.lm2, col="orange")
```



Residuals.

```
plot(fitted(doctors.lm2), resid(doctors.lm2),  
     pch=20, col="darkred")  
abline(h=0, col="orange", lty="dashed")
```

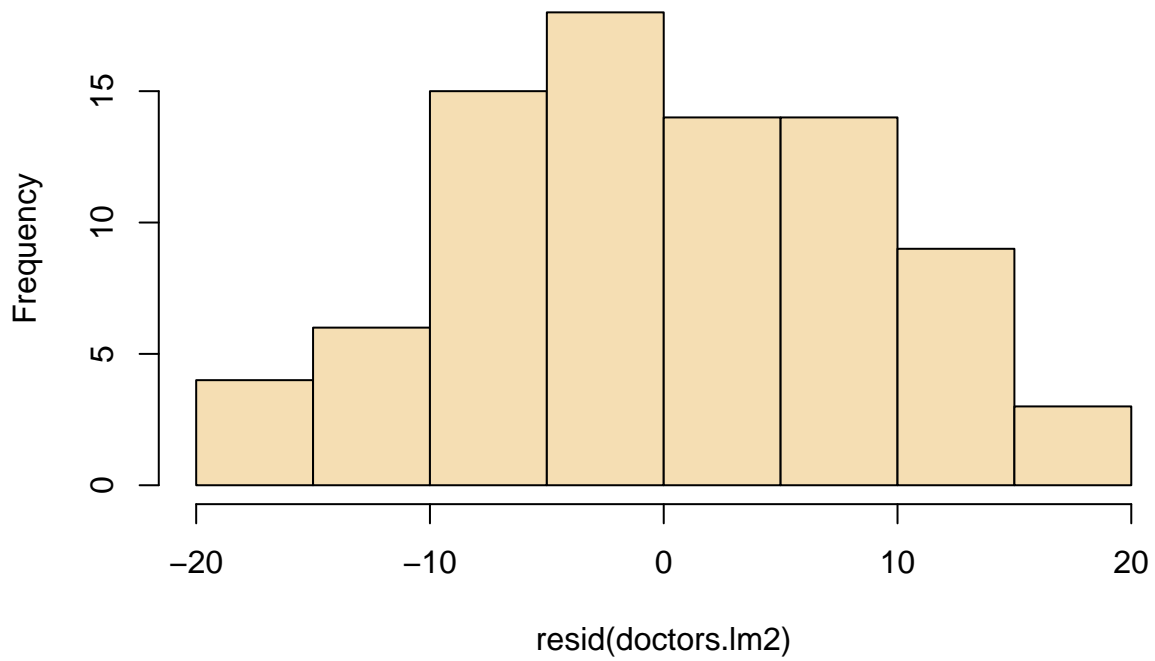


```
doctors.lm2
```

```
##  
## Call:  
## lm(formula = sqrt(NumMDs) ~ NumHospitals, data = data)  
##  
## Coefficients:  
## (Intercept) NumHospitals  
##      14.033      2.915
```

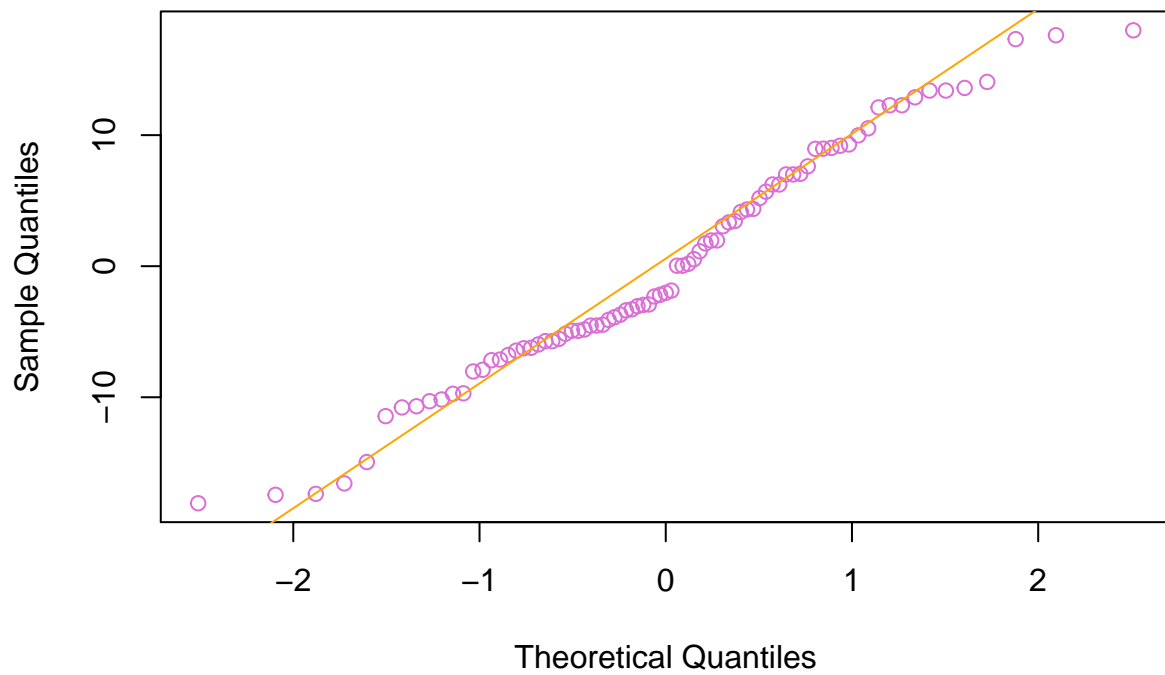
```
hist(resid(doctors.lm2), col="wheat")
```

Histogram of resid(doctors.lm2)



```
qqnorm(resid(doctors.lm2),  
        col="orchid")  
qqline(resid(doctors.lm2), col="orange")
```

Normal Q-Q Plot



Prediction.

```
new.data <- data.frame(NumHospitals=18)
y.hat <- predict(doctors.lm2, new.data)
NumMDs.hat <- y.hat^2
NumMDs.hat
```

```
##          1
## 4422.201
```

New linear model.

$$\widehat{NumMDs} = (-385.102 + 282.009 \cdot NumHospitals)^2$$

Illustration.

```
y.hat <- function(x){
  a <- 14.033
  b <- 2.915
  y.hat <- (a + b * x)^2
  return(y.hat)
}
plot(data$NumHospitals, data$NumMDs,
     pch=20, col="darkred")
curve(y.hat, from=2, to=30,
      col="olivedrab", add=TRUE)
```

